Robust deconvolution of transcriptomic samples using the gene covariance structure Bastien CHASSAGNOL



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Analysing the biological medium



01

A definition of cellular deconvolution



Standard deconvolution pipeline



Multivariate extension to standard deconvolution algorithms



Numerical simulation and future development

3

The complexity of the biological medium



Mixture of tissues Quon and Morris, 2009



Survey of the physical technics

to decipher the biological environment

Physical methods to analyse the biological medium

Before numerical deconvolution, dilemma between either characterising the individual cell populations (FACS, IHC) or getting a whole transcriptomic(RNASeq, microarray) overview.

Scenario A: increase of the gene expression is generated by an **activation** of cell population 1

infiltration of a new cell population 2

General principle of cellular deconvolution Deconvolution classes

Estimate the ratios *p* for all individuals with the purified cell signature **X** and bulk mixture **y**.

Try to infer cell specific expression profiles X

Partial deconvolution

- Complete deconvolution
- Try to infer alternatively both **p** and **X** (unsupervised, reference-free methods). Undetermined problem without prior.

based on **p** and **y**.

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Shen-Orr et al, 2013

Survey of the physical technics to decipher the biological environment

Co-regulated gene networks

Step 1: selection of cell types

Step 1: selection of cell types

Step 1: select relevant purified cellular expression profiles

Hematopoietic stem cell lineage

Automated cell ontology using *ontoProc* (Channing, 2022) package

Step 1: selection of cell types Step 1: selection of relevant datasets

Array accession	Cell types	Individuals	Samples	Phenotypes	Tissues	Citation
BluePrint	44	354	609	HC, tumoral	(cord) blood, thymus, bone marrow, tonsil, liver	Fernandez et al., 2016
E-MTAB-5640, the Immune Atlas	3	13	29	tumoral	kidney	Chevrier et al., 2017
ENCODE	9	13	37	HC	blood	Encode Project Consortium, 2012
GSE107011	27	13	123	HC	blood	Monaco et al, 2019
GSE137143	3	144	427	HC, auto immune	blood	Kim et al., 2021
GSE149050	4	91	223	HC, auto immune	blood	Panwar et al., 2021
GSE60424	4	20	80	HC, auto immune, Diabetes	blood	Linsley et al., 2014

7 reference RNASeq datasets of purified cell types, covering a large diversity of distinct cell populations (75 *unique cell types,* mostly immune cell types), in 8 *distinct tissues* (mostly whole blood) and both *healthy, tumoral and inflammatory* conditions.

Step 2: build a sparse transcriptomic network Step 2: learn the sparse GGM for each cell type

Step 2: build a sparse transcriptomic network

Filtering out noisy expression

Step 2: build a sparse transcriptomic network

17

5% threshold of the

expressed signal

Filtering out noisy expression

Step 2: build a sparse transcriptomic network Multivariate Gaussian Distributions

Spherical family

Diagonal family

General (or ellipsoidal) family *

Banfield and Raftery (1993) and Celeux and Govaert (1995)

Step 2: build a sparse transcriptomic network

Markov networks

Multivariate Gaussian distribution $f_{\zeta j}(\boldsymbol{X}) = \det(2\pi\Sigma_j)^{-\frac{1}{2}} \exp\left(-\frac{1}{2}(\boldsymbol{X}_i - \boldsymbol{\mu}_j)\boldsymbol{\Sigma}_j^{-1}(\boldsymbol{X}_i - \boldsymbol{\mu}_j)^{\top}\right), \quad \zeta_j = (\boldsymbol{\mu}_j, \boldsymbol{\Sigma}_j)$ Penalised Lasso (useful when N < G) $\boldsymbol{\Sigma}_j^{\text{Lasso}} = \arg\max_{\boldsymbol{\Sigma}_j} \ell_{\boldsymbol{\Sigma}_j}(\boldsymbol{X}_j) = \arg\max_{\boldsymbol{\Sigma}_j} \left[\underbrace{\log\left(\det\left(\boldsymbol{\Sigma}_j^{-1}\right)\right) - \underbrace{\boldsymbol{X}_j^{\top}}_{MLE} \boldsymbol{\Sigma}_j^{-1} \boldsymbol{X}}_{MLE} - \underbrace{\lambda ||\boldsymbol{\Sigma}_j^{-1} * (1 - \boldsymbol{W}_j)||_1}_{\text{Penalty term}} \right]$ Estimate a sparse covariance structure using gLasso (Friedman et al, 2008) algorithm

$$\Omega = \{\omega_{gl}, \text{ where } \Delta_{gl} = \rho_{gl}^A - \rho g l^B \neq 0\}$$

Differential network between conditions 1 and 2

- Activity scores: for each gene, sum of the z-scores of the *neighbour* differential values
- Neighbour: gene statistically differentially connected (permutation test) to our gene of interest

An overview of INDEED: input is transcriptomics data and the output is a prioritized ranked list gene based on the activity score defined within INDEED.

Step 2: build a sparse transcriptomic network From GGMs to GBNs

Sparse graphical GGM $\Theta = (\theta_{il}, (i, l) \in \{1, \dots, G\}) = \Sigma^{-1}$

+ Inverse of the sparse covariance structure (=precision matrix) has nice interesting properties, after some normalization $\rho_{i,l|V\setminus\{i,l\}} = -\frac{\theta_{il}}{\sqrt{\theta_{ii}\theta_{ll}}}$ $\forall (i,l) \in V, \quad X_i \perp \perp X_l \Leftrightarrow \rho_{i,l|V\setminus\{i,l\}} = 0$

- Estimator is shrunk: find asymptotically the good support (= the true zeros (*Meinshausen and Bühlmann*, 2006 // *Banerjee and other* 2007)) but the penalized estimator tends to underestimate true correlation)

Learn the MLE covariance matrix with constrained zeros

General formula from conditional distribution to global joined distribution, to retrieve the global multivariate Gaussian distribution.

Directed GBNs

- 1. Graph triangulation (adds a cord to any cycle above three vertices)
- 2. Hypothesis: from a triangular graph, able to orient the edges and learn the structure of a GBN
- 3. From the factorization of a GBN, learn easily the conditional distribution of each node to its parents

Step 2: build a sparse transcriptomic network GBNs (Gaussian Bayesian networks)

➡ Definition (Bayesian Network (BN))

A Bayesian network is a joint distribution over a set of random variables, defined with :

- a directed acyclic graph (DAG) G whose each node V_i ∈ V depicts a random variable X_i
- a global probability distribution X (with parameters Θ), admitting local factorisation for each variable X_i, depending only on its parents for each node PΠ_{X_i}.

Factorisation of the joint distribution in a BN

$$P(X_1, \cdots, X_n) = \prod_{i=1}^n P(X_i | \Pi_{X_i}) \text{ where } \Pi_{X_i} = \text{ parents of } X_i$$

As we have conditionally probability distribution, such a model respects normalisation constraint : $\sum_{i=1}^{n} P(X_i, \Pi_{X_i}) = 1$. Besides, local distribution for each variable X_i is represented by a CPT.

$$Product of Gaussian distributions$$
$$(X_1, \dots, X_k) \sim \mathcal{N} (\boldsymbol{\mu}, \boldsymbol{\Sigma})$$
$$\boldsymbol{\mu} = \left(\sum_{j=1}^J \boldsymbol{\Sigma}_j^{-1}\right)^{-1} \left(\sum_{j=1}^J \boldsymbol{\Sigma}_j^{-1} \boldsymbol{\mu}_j\right) \qquad \boldsymbol{\Sigma} = \left(\sum_{j=1}^J \boldsymbol{\Sigma}_j^{-1}\right)^{-1}$$

 $\begin{array}{c} \textbf{X1} \\ \textbf{X2} \\ \textbf{X1} \\ \textbf{X2} \\ \textbf{X3} \end{array} \qquad \begin{array}{c} \textbf{CD3} \quad \textbf{CD19} \quad \textbf{MHC-II} \\ \textbf{\sigma_1} \quad \textbf{0.5} \quad \textbf{0.8} \\ \textbf{\sigma_2} \quad \textbf{0} \\ \textbf{\sigma_3} \\ \textbf{MHC-II} \end{array} \qquad \begin{array}{c} \textbf{CD3} \\ \textbf{CD3} \\ \textbf{CD3} \\ \textbf{CD3} \\ \textbf{CD3} \\ \textbf{CD3} \\ \textbf{CD19} \\ \textbf{MHC-II} \end{array}$

 $\mathbb{P}(oldsymbol{X}_1,oldsymbol{X}_2,oldsymbol{X}_3)=\mathbb{P}(oldsymbol{X}_1|oldsymbol{X}_2,oldsymbol{X}_3)\mathbb{P}(oldsymbol{X}_3)\mathbb{P}(oldsymbol{X}_2)$

 $egin{aligned} From \ conditional \ to \ joint \ distribution \ X_1 &\sim \mathcal{N}_n \left(oldsymbol{\mu}, \Sigma
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Estimate cellular ratios Step 3: estimate the cell ratios

Batch effect

 Sequencing method (ssRNA-Seq, RNA-Seq, microarray)

Gene annotation and library

• Normalization (TPM, CPM, raw counts, ...)

Phenotypical conditions

 Heterotopic conditions (highly dependent on the tissue condition)

🔨 Tumoral environments

Poorly described tissues

Cellular distributions

Rare cell types

Model gene distributions
 (truncated and discrete by nature)

illover-effec

 Decorrelation between cell abundance and cell transcriptome

Main challenges to cope with cellular deconvolution

Estimate cellular ratios Main deconvolution categories for cellular ratios estimation

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Estimate the ratios from the reference signature and bulk mixture

Estimate cellular ratios

Bulk expression is computed as the weighted linear average of each purified cellular expression profile.

$$y_{gi} = \sum_{j=1}^{J} x_{gj} p_{ji}$$

algebraic form

matricial form

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Graphical model of the canonical linear regression modelling. The expression of a given gene in each cell population is supposed *fixed* and *independent* from the others.

Graphical model of our multivariate modelling: the observed variables are *stochastic*, and the genes *interplay* together.

Estimate cellular ratios Step 3: estimate the cell ratios

$$\hat{p}_i = \arg\min_{\hat{p}_i} ||\mathbf{X}\hat{p}_i - y_i||^2 \quad \hat{p}_i^{\text{OLS}} = (\mathbf{X}^\top \mathbf{X})^{-1} \mathbf{X}^\top \mathbf{y}_i \quad \hat{\mathbf{p}}_{\text{MLE}} = \arg\max_{\mathbf{p}} \left(\mathbb{P}_{\mathbf{p}}(y_{1:G}|\mathbf{X}_{1:G,1:J})\right) = \arg\max_{\mathbf{p}} \left(\prod_{g=1}^G \mathbb{P}_{\mathbf{p}}(y_g|\mathbf{x}_{.g})\right)$$

With the Gaussian-Markov assumptions, OLS is the best *BLUE* estimator and equal to the MLE estimate.

$$\ell_{\mathbf{y}|\mathbf{X},\boldsymbol{\Sigma}}(\mathbf{p}) = C + \log\left(\det\left(\sum_{j=1}^{J} p_{j}^{2}\boldsymbol{\Sigma}_{j}\right)^{-1}\right) - \frac{1}{2}(\mathbf{y} - \mathbf{X}\mathbf{p})^{\top} \left(\sum_{j=1}^{J} p_{j}^{2}\boldsymbol{\Sigma}_{j}\right)^{-1} (\mathbf{y} - \mathbf{X}\mathbf{p})$$

Deriving this quantity with *matrix calculus* is computable, but optimizing this quantity is intractable with non convex optimization (two local extrema, only one corresponding to the true MLE)

 $\frac{e^{p_j}}{\sum_{j=1}^{J-1} e^{p_j} + 1}, j < J \square$ Descent-gradient based method to learn the MLE. $\frac{1}{\sum_{j=1}^{J-1} e^{p_j} + 1}, j < J \square$ Parametrization (use of exponentials) to ensure the non-negativity and sum-to-one constraints (to be compared with *Lagrangian multiplier*)

Numerical simulation on artificial datasets

Simulation results with two genes

Numerical simulation on artificial datasets Simulation results with two genes

Same Heatmap representation as in the previous slide

Heatmap of the MSE of the estimated ratios, but using this time the covariance information

Conclusion

Data collection

Poorly described cell populations, full exploitation of Encode and Blueprint datasets

Automatic annotation and description of cellular ontology

Curation

Refine selection of relevant genes:

- Automated method for discarding background noise
- Innovative feature-selection algorithms, using both the differential expression and the covariance structure

Connectivity

Algorithm closer to biological models, accounting for the cotranscriptomic expression between the genes of the purified cell populations

Statistics

Statistical relevance of the estimates, possibly by means of a Bayesian framework.

Transcript distribution

AR1

Use of density functions closer to the gene distribution to model the counts

Environmental variation

Estimation of the impact of external phenotype features

Transcriptomic structure

Sparse transcriptomic network structure, estimated via MLE maximisation with constrained zeros imputed from gLasso

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A special thought to my tutors from Sorbonne University (LPSM, LIP6) for the theoretical background and to Servier for supplying internal data and automated pipeline for the analysis of transcriptomic data.

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Theory and packages

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Theory and packages

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